

Scholarship Examination

## MATHEMATICS II

23 February, 2022<br>Time allowed - 1 hour

## Show all working

Calculators may be used

1. On Tuesday 1 March I run 10 km . On Wednesday 2 March I run $20 \%$ further than I ran on Tuesday 1 March. On Thursday 3 March I run 10\% less than I ran on Wednesday 2 March. I continue this training programme, increasing by $20 \%$ on one day, and then decreasing by $10 \%$ on the following day. On what date will I first run more than 20 km ?
2. 



The diagram above shows three lines, $y=2 x, x+2 y=10$ and $y+3 x=20$, meeting at the points $A, B$ and $C$.
a. By solving the appropriate simultaneous equations, find the coordinates of the points $A, B$ and $C$.
b. Calculate the area of the triangle $A B C$.
3. The formula $n(n+1) / 2$ gives the sum of the integers between 1 and $n$ inclusive.

$$
\text { So } 1+2+3+\cdots+n=n(n+1) / 2
$$

For example, $1+2+3+4+5+6=6(6+1) / 2=21$
Using this formula for the sum of the integers between 1 and $n$ inclusive, find each of the following:
a. $1+2+3+\cdots+100$
b. $1+2+3+\cdots+200$
c. $101+102+103+\cdots+200$
d. $10+20+30+\cdots+1000$
e. $11+21+31+\cdots+1001$
f. $2+4+6+\cdots+200$
g. $1+3+5+\cdots+199$
4.


The diagram shows two equal shaded semicircles inside a larger semicircle. The larger semicircle has radius 2 cm . Calculate the area of one of the shaded semicircles, leaving your answer as a multiple of $\pi$.
5. a i Solve the equation $x^{2}-7 x+12=0$
ii Hence, or otherwise, solve the equation $(3 x-2)^{2}-7(3 x-2)+12=0$
b Solve the equation $\left(x^{2}-25\right)(x+7)-8 x(x+5)^{2}+5\left(x^{2}+5 x\right)+15(x+5)=0$
6.


Each week the junior civil servant in Downing Street wheels a suitcase to the local supermarket to buy alcohol. He always spends the same amount of money.

In week 1 he buys 10 bottles of gin, 5 bottles of vodka and 9 bottles of wine. In week 2 he buys 4 bottles of gin, 10 bottles of vodka and 12 bottles of wine. In week 3 he buys 2 bottles of gin and 27 bottles of wine.

In week 4 the Cabinet Secretary decrees that only vodka can be purchased. How many bottles of vodka can he buy?

